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Unsupervised Feature Selection and Learning for Image Segmentation

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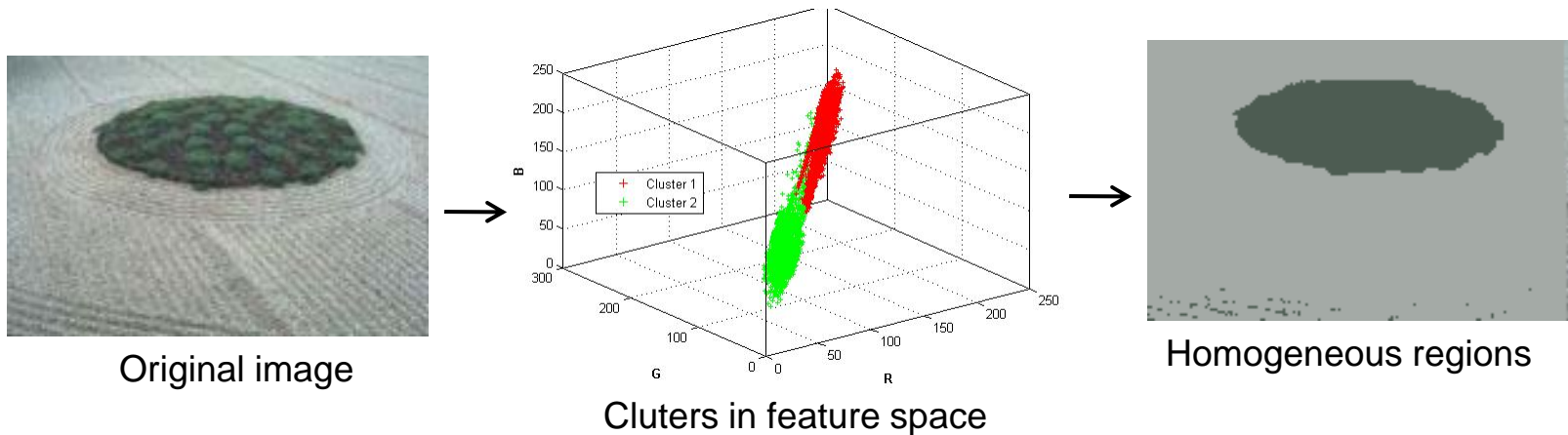
Plan

- Introduction
- Feature clustering for segmentation
- Feature selection for segmentation
- Some results
- Conclusions and future work

Introduction

Feature clustering is a popular approach for segmentation and grouping.

For **image segmentation**, clustering is performed in order to subdivide the feature space into **dense clusters**, which (presumably) correspond to **homogeneous regions** in the image.



Motivation of the problem

Finite Mixture models (FMM) has been proved as a powerful technique for clustering. It has been successfully used for segmentation.

FMM try to model the distribution of each cluster in the data using a **probability density function** (pdf).

The image data can then be described by a mixture of these densities.

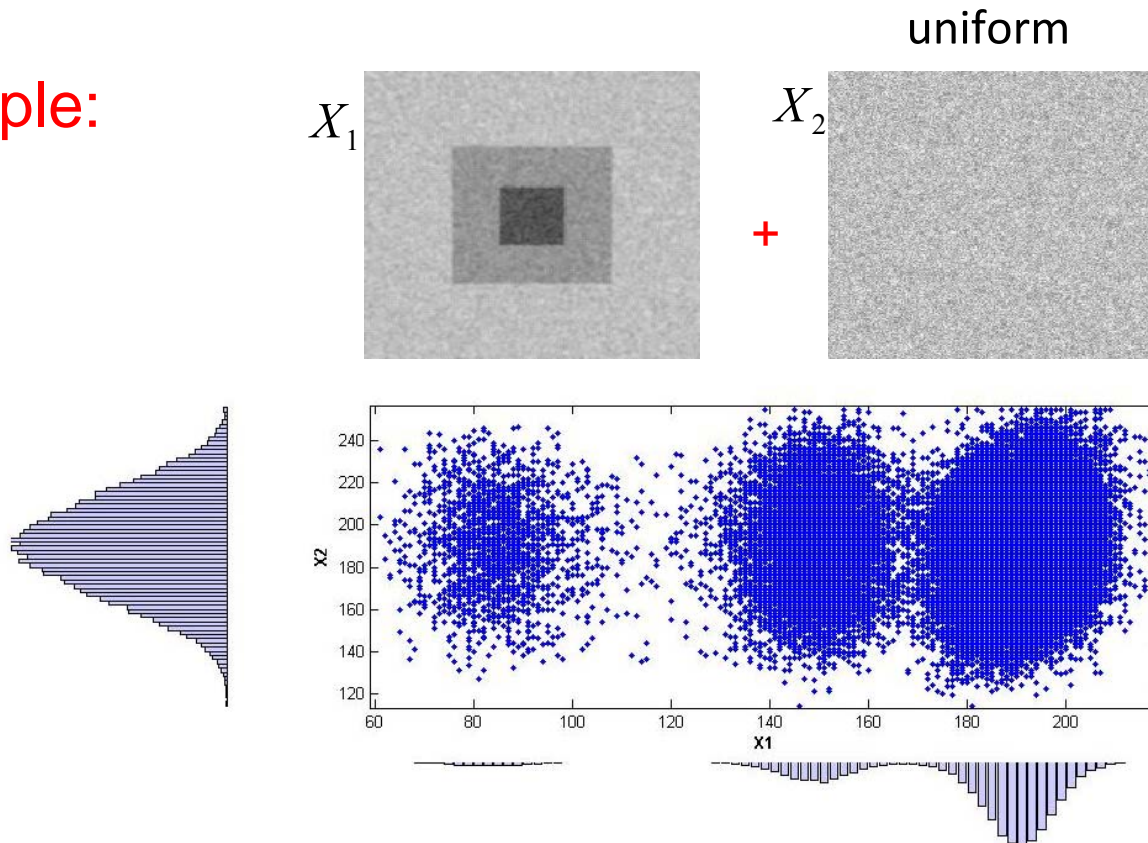
$$p(x) = \sum_{j=1}^K w_j \cdot p(x | \theta_j)$$

Motivation of the problem

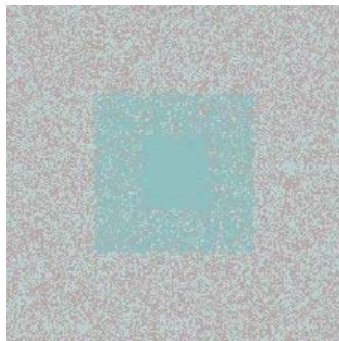
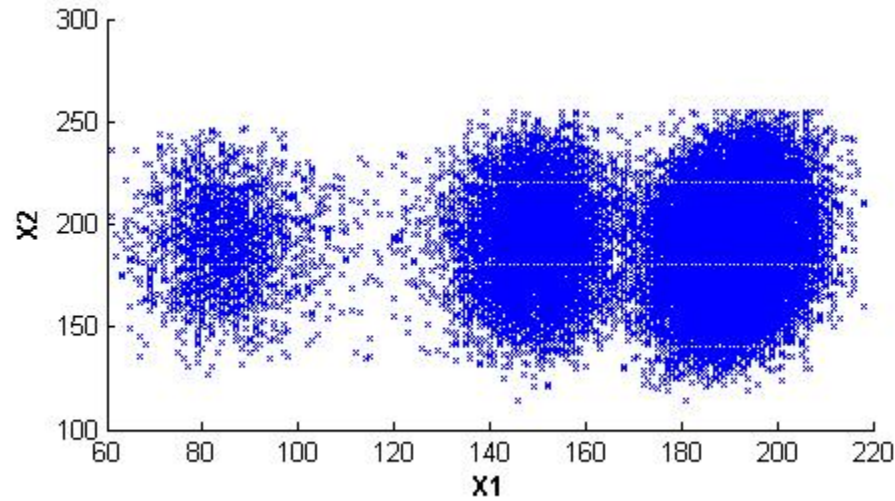
Motivation of the problem:

What is the best way to combine several features to yield optimal regions (clusters) in the image?

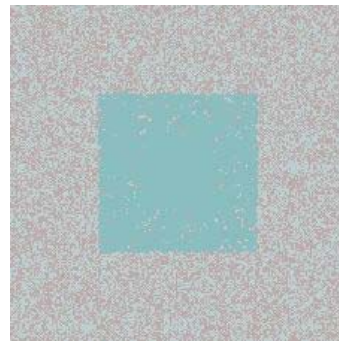
Example:



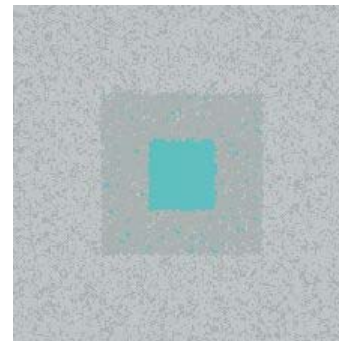
Motivation of the problem



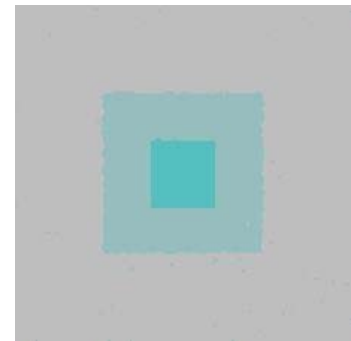
$$\alpha_1 = 0.3 \quad \alpha_2 = 0.7$$



$$\alpha_1 = 0.4 \quad \alpha_2 = 0.6$$



$$\alpha_1 = 0.5 \quad \alpha_2 = 0.5$$



$$\alpha_1 = 0.8 \quad \alpha_2 = 0.2$$

Motivation of the problem



CT

CR

EN

HG

VR

ICM

Proposed solution

Introduce feature selection (*saliency*) in segmentation.

We assume a feature vector $\vec{x} = (x_1, \dots, x_d)^T$ calculated from the image (composed of color and texture).

Without taking into account the feature *saliency*, the mixture model fitting the data is given by:

$$p(\vec{x}) = \sum_{j=1}^K w_j \cdot p(\vec{x} | \theta_j)$$

Proposed solution: Feature Selection (saliency)

The relevance of a feature is a random binary variable

$\phi_\ell \in \{0,1\}_{l=1}^d$. The distribution of ℓ th feature in component j is

$$p(x_\ell | \theta_{j\ell}, \varphi_\ell) \approx [p(x_\ell | \theta_{j\ell})]^{\phi_\ell} [p(x_\ell | \varphi_\ell)]^{1-\phi_\ell}$$

$p(x_\ell | \theta_{j\ell})$ and $p(x_\ell | \varphi_\ell)$ are 2 univariate general Gaussians.

Mixture of GGDs with feature selection

$p(\phi_\ell = 1)$ denotes the probability of relevance of the ℓ th feature

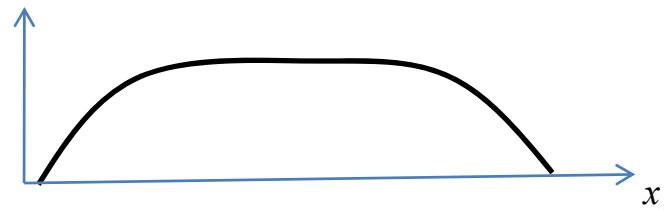
$$\rho_\ell = p(\phi_\ell = 1)$$

Now, the mixture model with feature selection becomes:

$$p(\vec{x}) = \sum_{j=1}^M w_j \prod_{\ell=1}^d [\rho_{\ell 1} p(x_\ell | \theta_{j\ell}) + (1 - \rho_{\ell 1}) p(x_\ell | \varphi_\ell)]$$

Use a secondary mixture to model the non-relevant features.

$$p(x_\ell | \varphi_\ell) = \sum_{k=1}^K \pi_k p(x_\ell | \varphi_{k\ell})$$



Mixture of GGDs with feature selection

We end up with the following general model:

$$p(\vec{x}) = \sum_{j=1}^M w_j \prod_{\ell=1}^d \left[\rho_{\ell 1} p(x_{\ell} | \theta_{j\ell}) + (1 - \rho_{\ell 1}) \left(\sum_{k=1}^K \pi_{k\ell} p(x_{\ell} | \varphi_{j\ell}) \right) \right]$$

Problem:

Estimate the model parameters (θ, φ, K, M) ?

Model selection

Solution: Use the minimum message length principle:

$$(\Theta^*, M^*, K^*) = \arg \min_{\Theta, M, K} \{ \text{MessLen}(\Theta, M, K) \} \quad \Theta = (\theta, \varphi)$$

$$\text{MessLen} = -\log p(\Theta) - \log p(X | \Theta) + \frac{1}{2} \log |I(\Theta)| + \frac{c}{2} (1 - \log(12))$$

$c = M + d + 3dM + 4dK$ is the total number of parameters

Model Learning

We use the Expectation - Maximization (EM) algorithm to minimize iteratively *MessLen* w.r.t (Θ, K, M) .

Over - initialize EM with

$$M = M_{\text{Max}} \text{ and } K = K_{\text{Max}}.$$

After convergence, find optimal values of (K, M) and Θ including the relevance of the features ρ_ℓ .

Performance testing

Boundary alignment error (ε_1):

$$\varepsilon_1 = \frac{1}{N} \sum_{(u,v) \in I} \min\{\varepsilon_{u,v}(S_G, S_T), \varepsilon_{u,v}(S_T, S_G)\}$$

where $\varepsilon_{u,v}(S_G, S_T) = \frac{|S_G - S_T|}{|S_G|}$ and $\varepsilon_{u,v}(S_T, S_S) = \frac{|S_T - S_G|}{|S_T|}$

Amount of over/under-segmentation (ε_2):

$$\varepsilon_2 = \# \text{ of over - segmented segments.}$$

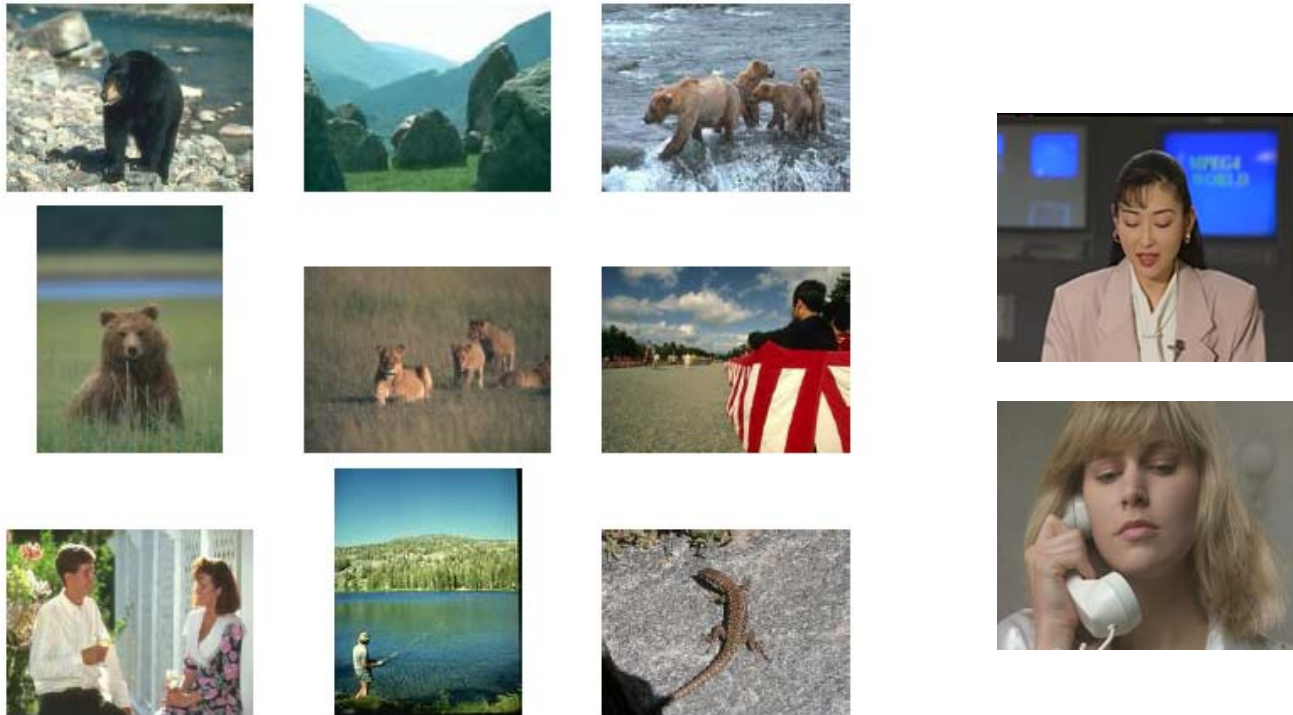
S_G : Segment in the ground truth.

S_T : Segment in a tested segmentation.

Some results

We tested our model for image and video segmentation.

We used the Berkeley Benchmark dataset and known test videos:



Some results

MoG

MoG+FS

MoGG

MoGG+FS(K=1)

MoGG+FS(K*)



K=2



K=1



K=1



K=1

Some results



Some results

Image segmentation

$[\bar{\epsilon}_1, \bar{\epsilon}_2]$				
MoG	MoG+FS	MoGG	MoGG+FS (K=1)	MoGG+FS (K=*)
[0.21, 23]	[0.15, 16]	[0.19, 20]	[0.13, 13]	[0.10, 11]

Video segmentation

Video	Size	$[\bar{\epsilon}_1, \bar{\epsilon}_2]$				
		MoG	MoG+FS	MoGG	MoGG+FS(K=1)	MoGG+FS(K=*)
Akiyo	300 frames	[0.23,22.5]	[0.16,17.8]	[0.22,20.5]	[0.12,13.2]	[0.12,13.2]
suzie	150 frames	[0.25,27.4]	[0.18,19.1]	[0.24,23.7]	[0.15,17.5]	[0.12,11.3]
Grandma	870 frames	[0.19,20.5]	[0.15,14.8]	[0.17,19.3]	[0.13,14.5]	[0.12,13.9]
Irene	300 frames	[0.27,28.2]	[0.19,20.8]	[0.23,26.6]	[0.16,17.3]	[0.13,14.4]

Conclusion and future work

- We introduced an unsupervised model for feature selection and clustering for segmentation.
- Feature selection is important for mitigating over-segmentation due to uniform (non-relevant) features.
- Use more features for more accurate segmentation.
- Use feature selection for object segmentation.

Thank you!

Questions?